## Overview of Neural Network Approaches in the Localization of Stochastic EM Sources

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Abstract - In this paper we present a brief overview of the results achieved in the field of application of artificial neural networks for a spatial localization of stochastic EM radiation sources. The theory of stochastic sources near-field representation in the form of antenna arrays with dipole elements and correlation matrix calculation in the far-field scan area as well as the architecture of developed neural models for the 1D and 2D DoA estimation are brefly presented here. Scenarios when sources are moving along one direction and where their position is determined by only one protrusion angle in relation to the linear antenna array and when stochastic springs move in a plane that is parallel to the rectangular antenna array so that their position is determined with two spatial angles are both considered in the paper. In addition, a few example are given to ilustrate the presented neural model capability to efficiently perform the DoA estimation for either uncorrelated or partially correlated sources.

*Keywords* – Source localization, Stochastic radiation, Moveable sources, Correlation matrix, Neural networks.

### I. INTRODUCTION

Today, there are many techniques aiming to improve the performances of different wireless communication systems. One of them is a technique based on antenna arrays with adaptive beamforming capabilities [1,2]. It offers possibilities to minimize or even eliminate interferences and to enhance information signals at the reception by using antennas with radiation pattern optimized from the knowledge of interference sources positions. Location of unwanted signal sources are usually determined by employing some of the available DoA (Direction of Arrival) estimation algorithms, e.g. MUSIC [1-3]. These algorithms are usually very accurate but majority of them require complex and hardware- and timeconsuming mathematical operations which limit their applications in real working environment. One possible alternative to these algorithms is based on using artificial neural networks (ANNs) [4-16]. They provide the DoA estimation of almost same precision as e.g. MUSIC but with much faster run-time due to avoidance of exhausting calculations.

Authors of this paper have considered in the past the application of ANNs for the one dimensional (1D) and two-

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dimensional (2D) DoA estimation of deterministic electromagnetic (EM) radiation sources [4-6]. Stochastic EM sources have to be also considered from the interference point of view [17,18] and their angular positions have been determined by using the ANN models developed by the authors of this paper in [7-14]. In [7-12], authors have proposed the neural model for the 1D DoA estimation of moving stochastic sources whose locations were characterized only by one angular coordinate (azimuth). In [7-9] neural models for the DoA estimation of either single or multiple uncorrelated stochastic sources were developed while in [10] an enhancement of these models was done in order to be able to first determine the number of sources present in the monitoring space and then perform the DoA estimation. In [11-12] neural models for 1D DoA estimation of stochastic sources, which are mutually partially correlated, were proposed. Also in [13,14] neural models for 2D DoA estimation were developed. In [13], the model was applied to determine two angular spatial coordinates of one stochastic source, and in [14] for determining angular coordinates of two uncorrelated stochastic sources moving in 2D space (plane).

## II. STOCHASTIC SOURCE LOCATION BASED ON 1D DOA ANN MODELING

## *II.A. Correlation matrix calculation for 1D source movement*

In [17,18], a stochastic source was modelled by a uniform antenna array with *N* dipole elements at mutual distance equal to the half of the operating wavelength (Fig.1). The level of correlation between dipoles feed currents  $\mathbf{I}=[I_1, I_2, ..., I_N]$ ),  $\mathbf{c}^I(\omega)$ , describing the noisy source radiation, is of the form [17,18]:

$$\mathbf{c}^{I}(\omega) = \lim_{T \to \infty} \frac{1}{2T} \Big[ I(\omega) I(\omega)^{H} \Big]$$
(1)

To find the total electric field in the far-field sampling point, vector **M**, comprising the contribution of each antenna array element with radiation pattern  $F(\theta)$ , is needed:

$$\mathbf{M}(\theta) = jz_0 \frac{F(\theta)}{2\pi r} \left[ \frac{e^{jkr_1}}{r_1} \quad \frac{e^{jkr_2}}{r_2} \dots \frac{e^{jkr_N}}{r_N} \right]$$
(2)

$$E(\theta) = \mathbf{M}(\theta)\mathbf{I} \tag{3}$$

where  $z_0$  and k are free-space impedance and phase constant, respectively,  $r_1$ ,  $r_2$ , ...,  $r_N$  are the distances between the far-



field sampling point and antenna array elements and  $E(\theta)$  is the total electric field intensity in sampling point in far-field positioned at angle  $\theta$  in azimuth plane with the respect to the first element of antenna array. If there are *M* sampling points in the far-field, then notation  $r_{i,m}$ , representing the distance between *i*-th element  $(1 \le i \le N)$  in the antenna array and *m*-th sampling point in the far-field  $(1 \le m \le M)$  (see Fig. 1), can be used. Position of these points  $(Y_1 Y_2, ..., Y_M)$  in the far-field, is described by the azimuth plane angles  $(\theta_i)$ ,  $(\theta), ..., (\theta_M)$ , determined as previously said with the respect to the first element of antenna array. The correlation matrix of signals sampled at these points can be calculated as:

$$\mathbf{C}_{E}[i,j] = \mathbf{M}(\theta_{i})\mathbf{c}^{I}\mathbf{M}(\theta_{j})^{H}$$

$$i = 1 \qquad M \qquad i = 1 \qquad M \qquad (4)$$

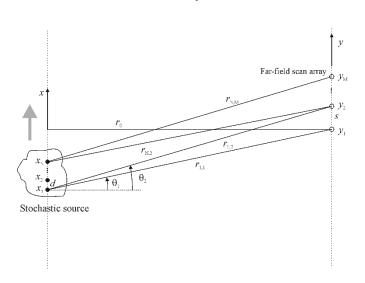


Figure 1: The position of stochastic source in azimuth plane with respect to the location of EM field sampling points in the far-field scan area [8].

For the multiple stochastic sources in the azimuth plane, the level of EM field and the elements of correlation matrix  $C_E$  in particular far-field sampling point, are calculated by the superposition of radiation field from all sources. If there are *S* stochastic sorces, then the vector M has a form [8]:

$$\mathbf{M}(\theta) = jz_0 \frac{F(\theta)}{2\pi} \cdot \left[ \frac{e^{jkr_1^{(1)}}}{r_1^{(1)}} \cdots \frac{e^{jkr_N^{(1)}}}{r_N^{(1)}} \frac{e^{jkr_1^{(2)}}}{r_1^{(2)}} \cdots \frac{e^{jkr_N^{(2)}}}{r_N^{(2)}} \cdots \frac{e^{jkr_1^{(S)}}}{r_1^{(S)}} \cdots \frac{e^{jkr_N^{(S)}}}{r_N^{(S)}} \right]$$
(5)

where  $r_i^{(j)}$  is the distance between *i*-th element in antenna array, representing *j*-th stochastic source, and the sampling point in far-field, while the feed currents vector is:

$$\mathbf{I} = \begin{bmatrix} I_1^{(1)} \dots I_N^{(1)} & I_1^{(2)} \dots I_N^{(2)} \dots & I_1^{(S)} \dots & I_N^{(S)} \end{bmatrix}$$
(6)

where  $I_i^{(j)}$  is the feed current of *i*-th element in antenna array representing *j*-th stochastic source [8].

By using Eqs.(3-6), the EM field in the sampling point in the far-field, as well as the elements of correlation matrix  $C_E$ 

can be obtained. In addition, if unknown, matrix  $\mathbf{c}^{I}(\omega)$  can be determined by measuring the electric field in the near-field of stochastic source [8].

### II.B. Neural model for 1D DoA estimation

The neural model, based on MLP ANN, is trained to extract information about position of *S* stochastic sources in azimuth plane from the correlation matrix  $C_E$  [8]:

$$\boldsymbol{\theta} = f(\mathbf{C}_{E}) \tag{7}$$

In Eq.(7), vector  $\boldsymbol{\theta}$  is azimuthal angle vector of stochastic sources,  $\boldsymbol{\theta} = [\theta_1, \theta_2, \dots, \theta_s]$ , while the elevation coordinates of radiation sources position are in this case neglected. The architecture of developed neural model is shown in Fig.2 and it can be represented as:

$$\mathbf{y}_l = F(\mathbf{w}_l \mathbf{y}_{l-1} + \mathbf{b}_l) \quad l = 1, 2$$
(8)

where  $\mathbf{y}_{l-1}$  vector describes the output of (l-1)-th hidden layer,  $\mathbf{w}_l$  is a connection weight matrix among (l-1)-th and lth hidden layer neurons and  $\mathbf{b}_l$  is a vector containing biases of l-th hidden layer neurons [8].. F is the activation function of neurons in hidden layers and in this case it is a hyperbolic tangent sigmoid transfer function:

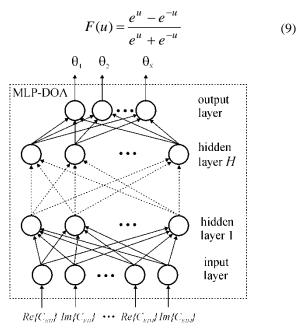


Figure 2: Architecture of MLP neural model for 1D DOA estimation of stochastic EM source signal in azimuth plane [8]

In order to perform mapping it is sufficient to take only the first column of correlation matrix and therefore  $\mathbf{y}_0 = [Re\{\mathbf{C}_{\mathrm{E}}[1,1]\}\ Im\{\mathbf{C}_{\mathrm{E}}[1,1]\}, \dots, Re\{\mathbf{C}_{\mathrm{E}}[1,M]\}\ Im\{\mathbf{C}_{\mathrm{E}}[1,M]\}].$ Also,  $\boldsymbol{\theta}$  is given as  $\boldsymbol{\theta} = \mathbf{w}_3\mathbf{y}_2$  where  $\mathbf{w}_3$  is a connection weight matrix between neurons of last hidden layer and neurons in output layer [8].. The optimization of weight matrices and biases values during the training allows ANN to



approximate the mapping with the wanted accuracy. The general designation for the MLP neural model is MLP*H*- $N_1$ - $\dots$ - $N_i$ - $\dots$ - $N_H$  where *H* is the total number of hidden layers used MLP network, while  $N_i$  is the total number of neurons in the *i*-th hidden layer.

# *II.C. 1D DoA estimation - modelling results for uncorrelated sources*

The application of neural model for the 1D DoA estimation of uncorrelated stochastic sources will be illustrated here on the example of two moveable sources (S=2). The training of ANN is conducted when there are four equidistant sampling points (M=4) in the far-field scan area, at the mutual distance  $d = \lambda/2$ , located 100 m from stochastic sources (Table I) [8]. Angular position in the azimuth plane of two sources at arbitrary angle distance will be determined from the correlation matrix information in the far field scan area. Each of two stochastic sources is described by antenna array with four dipole elements (N=4). The feed currents of four dipole elements are mutually uncorrelated so that  $\mathbf{c}^{I}$  is the unit diagonal matrix. By using Eqs.(4-5) for N=4 and M=4, 861 and 276 uniformly distributed samples are generated for training and testing, respectively, in the range [-80° 80°] at the working frequency of 7.5 GHz. Levenberg-Marquartd method with prescribed accuracy of 10<sup>-4</sup> is used as a training algorithm. The testing results for six MLP models with the lowest average case error are shown in Table II, and MLP2-16-8 is chosen as representative neural model.

 TABLE I

 The values of parameters used in sampling process [8].

Frequency	<i>f</i> = 7.5 GHz
Number of sources	S = 2
Number of antenna array elements per one source	N = 4
Sampling points distance from source trajectory	$r_0 = 100 \text{ m}$
Number of sampling points	M = 4
Mutual distance of the sampling points	$s = \lambda/2 \; (0.02 \text{ m})$

 TABLE II

 Testing results for six MLP neural models with the best average errors statistics [8].

MLP model	WCE [%]	ACE [%]
MLP2-16-8	1.81	0.42
MLP2-14-14	2.26	0.42
MLP2-18-14	2.67	0.39
MLP2-20-10	2.71	0.38
MLP2-16-16	3.27	0.39
MLP2-16-11	3.76	0.41

The neural model simulation of testing samples set shows a very good agreement between the output values of neural model and referent azimuth values for two sources (Fig.3 and Fig.4) [8]. In addition, a good agreement with results obtained by MUSIC algorithm can be observed.

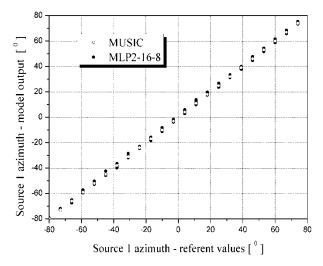


Figure 3: Comparison of MLP2-16-8 model output 1 (azimuth of source 1) with MUSIC and referent azimuth values [8].

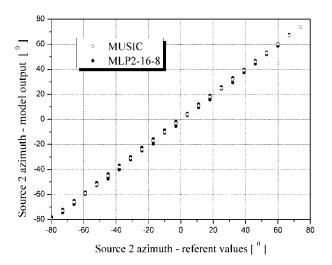


Figure 4: Comparison of MLP2-16-8 model output 2 (azimuth of source 2) with MUSIC and referent azimuth values [8].

## *II.D. 1D DoA estimation - modelling results for partially correlated sources*

MLP neural model, whose architecture was presented in II.A section, can be also applied for 1D DoA estimation of partially correlated stochastic sources. This capability will be illustrated for two EM sources (*S*=2) that independently move along linear trajectory distant  $r_0 = 100$  m from the antenna array, with whom the signal is sampled at frequency f = 28 GHz [11]. Each stochastic source is represented by a dipole (*N*=1) whose axis is normal on the azimuthal plane.



The scanning width of antenna array in the azimuth is  $[-30^{\circ}]$ . Partial correlation between sources is:

$$\mathbf{c}^{I} = \begin{bmatrix} 1 & c_{12}^{I} \\ c_{21}^{I} & 1 \end{bmatrix}$$
(10)

where  $c = c_{12}^{I} = c_{21}^{I}$  is in the range  $0.05 \le c \le 0.8$  [11. If sources are uncorrelated then *c* is equal to zero. For partially correlated and uncorrelated cases we generated separate sample sets for network training and testing, while using common parameters of sampling that are given in Table III [11].

For training and testing samples generation we use relations (4) and (5) that establish inverse mapping from that of the MLP DoA model

$$\mathbf{C}_{E}^{t} = f_{DoA}^{-1} \left( \theta_{1}^{t}, \theta_{1}^{t}, c \right) \tag{11}$$

Samples for neural network training and testing are given in the format {( $\mathbf{x}^{t}(\theta^{t}_{1}, \theta^{t}_{2}, c^{t}), \theta^{t}_{1}, \theta^{t}_{2}$ )}, where  $\mathbf{x}^{t}$  is vector of input model values  $\mathbf{x}^{t} = [Re\{\mathbf{C}_{E}^{t}[1,1]\},..., Re\{\mathbf{C}_{E}^{t}[1,M]\},$  $Im\{\mathbf{C}_{E}^{t}[1,1]\},..., Im\{\mathbf{C}_{E}^{t}[1,M]\}]^{T}$ . For each element of vector  $\mathbf{x}^{t}$  we used uniform distribution of samples for azimuth angles of radiation source location and correlation of the form  $[\theta^{t}_{min} : \theta^{t}_{step} : \theta^{t}_{max}]$  and  $[c^{t}_{min} : c^{t}_{step} : c^{t}_{max}]$ , where  $\theta^{t}_{min}$  [°] and  $c^{t}_{min}$ represent the lowest limit of distribution,  $\theta^{t}_{max}$  [°] and  $c^{t}_{step}$ represent uniform sampling steps [11].

 TABLE III

 The values of parameters used in sampling process [11]

Frequency	f = 28  GHz
Number of sources	S = 2
Number of antenna array elements per one source	N = 1
Sampling points distance from linear source trajectory	$r_0 = 100 \text{ m}$
Number of sampling antenna array sensors	M = 6
Mutual distance of the antenna sensors	$s = \lambda/2$ (5.4 mm)

For neural model training and testing in the uncorrelated case the following sets were generated [11]:

TRAINING\_A set (28920 samples):

$$\begin{cases} (\mathbf{x}^{t}(\theta_{1}^{t},\theta_{2}^{t},0),\theta_{1}^{t},\theta_{2}^{t}) | \\ \theta_{1}^{t} \in [-30:0.25:30], \theta_{2}^{t} \in [-30:0.25:30], \theta_{1}^{t} > \theta_{2}^{t} \end{cases}$$
(12)

TEST\_A set (5050 samples):

$$\begin{cases} (\mathbf{x}^{t}(\theta_{1}^{t}, \theta_{2}^{t}, 0), \theta_{1}^{t}, \theta_{2}^{t}) \mid \\ \theta_{1}^{t} \in [-30: 0.6: 30], \theta_{2}^{t} \in [-30: 0.6: 30], \theta_{1}^{t} > \theta_{2}^{t} \end{cases}$$
(13)

For neural model training and testing in the partially correlated case the following sets were generated:

TRAINING\_B set (29280 samples):

$$\begin{cases} (\mathbf{x}^{t}(\theta_{1}^{t},\theta_{2}^{t},c^{t}),\theta_{1}^{t},\theta_{2}^{t}) \mid \\ \theta_{1}^{t} \in [-30:1:30], \theta_{2}^{t} \in [-30:1:30], \theta_{1}^{t} > \theta_{2}^{t}, \\ c^{t} \in [0.05:0.05:0.8] \end{cases}$$
(14)

TEST\_B set (3036 samples):

$$\begin{cases} (\mathbf{x}^{t}(\theta_{1}^{t}, \theta_{2}^{t}, c^{t}), \theta_{1}^{t}, \theta_{2}^{t}) \mid \\ \theta_{1}^{t} \in [-30: 2.7: 30], \theta_{2}^{t} \in [-30: 2.7: 30], \theta_{1}^{t} > \theta_{2}^{t}, \\ c^{t} \in [0: 0.07: 0.8] \end{cases}$$
(15)

Samples in the TRAINING\_A and TEST\_A sets were generated under conditions of uncorrelated radiation of two stochastic sources while the samples in the TRAINING\_B set are generated under conditions of partial correlation in the range  $0.05 \le c \le 0.8$ . Set TEST\_B contains samples that are generated also under variable radiation correlation in above range but also it has samples that are generated under no correlation. Different number of MLP ANNs with two hidden layers (H = 2) and different number of neurons in them (MLP2- $N_1$ - $N_2$ ,  $4 \le N_1$ , $N_2 \le 23$ ) were considered during the training, For the testing the values of worst case error (WCE) and average error (ACE) [4,5] were taken into account for model accuracy estimation.

After training the MLP neural models with the set TRAINING\_A, the results of the testing of the six models with lowest value of WCE on the set TEST\_A are shown in Table IV [11]. Figs. 5(a) and 5(b) [11] present a scattering diagram of MLP2-12-7 model on TEST\_A set (this model has shown lowest WCE on that set). It can be seen that all six models show high accuracy in source location estimation. But if in the network input we deliver samples that are generated with some source radiation correlation (set TEST\_B) then the models show a high WCE value or high imprecision in source location estimation. That may be seen also in Table IV [11] also from scattering diagram of MLP2-12-7 model on TEST\_B set (Figs 6(a) and 6(b)) [11].

 TABLE IV

 Testing results for six MLP neural models trained on

 TRAINING\_A set with the best average errors statistics [11]

MLP model	TEST_A set		TEST_B set	
NILF model	WCE [%]	ACE [%]	WCE [%]	ACE [%]
MLP2-12-7	2.25	0.36	60.63	6.76
MLP2-13-13	2.26	0.38	87.81	6.01
MLP2-11-4	2.38	0.37	87.31	7.16
MLP2-16-16	2.43	0.37	59.02	6.07
MLP2-12-12	2.51	0.37	89.37	7.17
MLP2-12-5	2.55	0.37	83.99	6.91

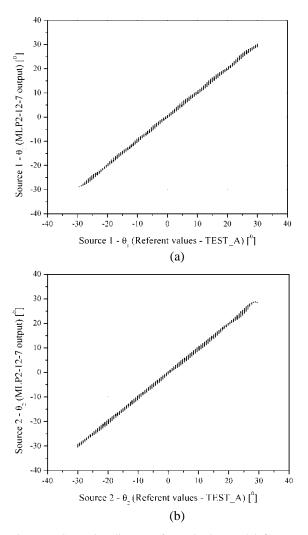


Figure 5: Scattering diagram of MLP2-12-7 model  $\theta_l$  output (a), and  $\theta_2$  output (b), on TEST\_A set [11]

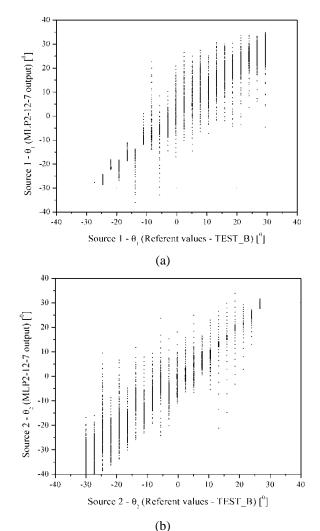
After training MLP neural models on the set TRAINING\_B, the results from testing of six models with lowest value for WCE on set TEST\_B are shown in Table V [11]. In Figs. 7(a) and 7(b) [11] we may see scattering diagram of the MLP2-22-22 model on the set TEST\_B (this model has shown lowest value of WCE on that set). It can be seen that the model MLP2-22-22 has a satisfactory accuracy in angle position determination when we use samples for different partial correlations of sources.

 TABLE V

 Testing results for six MLP neural models trained on

 TRAINING\_B set with the best average errors statistics [11]

MLP model	TEST_B set	
WILF model	WCE [%]	ACE [%]
MLP2-22-22	4.53	0.35
MLP2-23-23	5.58	0.33
MLP2-22-20	5.70	0.36
MLP2-18-16	5.74	0.36
MLP2-18-18	6.33	0.34
MLP2-16-16	8.27	0.35



(0)

Figure 6: Scattering diagram of MLP2-12-7 model  $\theta_l$  output (a), and  $\theta_2$  output (b), on TEST\_B set [11]

### III. STOCHASTIC SOURCE LOCATION BASED ON 2D DOA ANN MODELING

## *III.A. Correlation matrix calculation for 2D source movement*

For 2D movement scenarios, Eqs.(2-3) have to be modified [14]:

$$\mathbf{M}(\theta,\varphi) = jz_{0} \frac{F(\theta,\varphi)}{2\pi} \cdot \left[ \frac{e^{jkr_{1}^{(1)}}}{r_{1}^{(1)}} \cdots \frac{e^{jkr_{N}^{(1)}}}{r_{N}^{(1)}} \frac{e^{jkr_{1}^{(2)}}}{r_{1}^{(2)}} \cdots \frac{e^{jkr_{N}^{(2)}}}{r_{N}^{(2)}} \cdots \frac{e^{jkr_{1}^{(S)}}}{r_{1}^{(S)}} \cdots \frac{e^{jkr_{N}^{(S)}}}{r_{N}^{(S)}} \right]$$
(16)  
$$E(\theta,\varphi) = \mathbf{M}(\theta,\varphi)\mathbf{I}$$
(17)

where  $r_i^{(j)}$  is the distance between *i*-th element in antenna array, representing *j*-th stochastic source, and the sampling point in far-field. The correlation matrix of signals received



in these sampling points can be obtained from the correlation matrix of antenna elements feed currents as [14]:

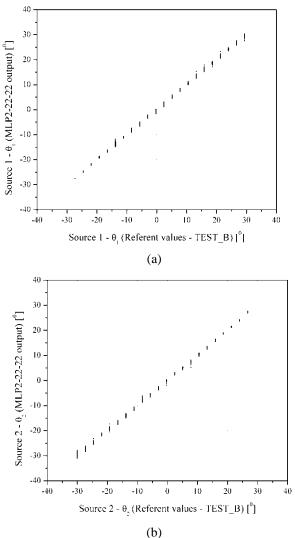


Figure 7: Scattering diagram of MLP2-22-22 model  $\theta_1$  output (a), and  $\theta_2$  output (b), on TEST\_B set [11]

$$\mathbf{C}_{E}[i, j] = \mathbf{M}(\theta_{i}, \varphi_{i})\mathbf{c}^{T}\mathbf{M}(\theta_{j}, \varphi_{j})^{H}$$

$$i = 1, ..., M \quad j = 1, ..., M$$
(18)

Spatial angles  $\theta$  and  $\varphi$  in Eqs.(16) and (17)  $\theta$  describe stochastic source location with respect to the selected sampling point in far-field,  $F(\theta,\varphi)$  is the radiation characteristic of the antenna array element and  $r_s$  the distance between s-th stochastic EM source and selected sampling point. When a rectangular antenna array of dimensions  $M \times P$  is used at the reception, the far-field sampling points correspond to the positions of elements of this array and their total number will be  $K=M \cdot P$ . In our scenario shown in Fig.8, S stochastic sources are moving independently from each other in a plane parallel to the rectangular antenna array [14]. Axes of dipoles representing stochastic sources are lying in the plane in which sources are moving and they are parallel to the x-axis so that their radiation in the direction of sampling points can be approximated with isotropic radiation. The distance between elements of receiving antenna array along the x-axis is dx,

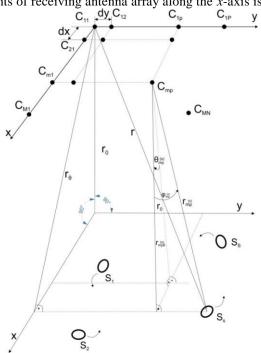


Figure 8: The position of stochastic EM sources in *x-y* plane with respect to the location of sampling points in the far-field scan area [14].

while the distance between elements along the y-axis is dy. The distance between the plane of planar receiving antenna array and the plane in which stochastic sources are moving is  $r_0$ . When the mapping from Eq.(18) is applied separately on each of the sampling points, the appropriate distance between *s*-th stochastic source and the sampling point at the position of (m,p) sensor of planar receiving array is [14]:

$$r_{mp}^{(s)} = \frac{r_0}{\cos\varphi_{mp}^{(s)}\cos\theta_{mp}^{(s)}}$$
(19)

where  $r_0$  represents the distance between the plane of planar receiving antenna array and the plane is which *S* stochastic sources are moving, while  $\theta_{mp}^{(s)}$  and  $\varphi_{mp}^{(s)}$  are spatial angles related to the position of *s*-th source with respect to the (m,p) sensor position and they are [14]:

$$\theta_{mp}^{(s)} = \arctan\left[\tan\theta_{11}^{(s)} - \frac{(m-1)\cdot dx}{r_0}\right]$$
(20)

$$\varphi_{mp}^{(s)} = \arctan\left[\tan\varphi_{11}^{(s)} - \frac{(p-1)\cdot dy}{r_0}\right]$$
 (21)

where  $\theta_{II}^{(s)}$  and  $\varphi_{II}^{(s)}$  are spatial angles related to the position of *s*-th source with respect to the referent (1,1) position of antenna array (referent sensor of array). Angles  $\theta_{II}^{(s)}$  and  $\varphi_{II}^{(s)}$  represent at the same time the angular  $(\theta, \varphi)$ 



position of *s*-th stochastic source with respect to the planar receiving antenna array so that  $\theta_{II}^{(s)} = \theta$  and  $\varphi_{II}^{(s)} = \varphi$ .

Correlation matrix of signals in sampling points is defined as [14]:

$$\widetilde{\mathbf{C}}_{E}[i,j] = \mathbf{M}(\theta_{\left(\left[\frac{i}{p}\right]+1\right)\left(i-\left[\frac{i}{p}\right]\right)}, \varphi_{\left(\left[\frac{j}{p}\right]+1\right)\left(i-\left[\frac{j}{p}\right]\right)})\mathbf{c}^{t}\mathbf{M}(\theta_{\left(\left[\frac{j}{p}\right]+1\right)\left(j-\left[\frac{j}{p}\right]\right)}, \varphi_{\left(\left[\frac{j}{p}\right]+1\right)\left(j-\left[\frac{j}{p}\right]\right)})^{t}$$
$$i = 1, \dots, K \quad j = 1, \dots, K \quad K = M \cdot P \qquad (22)$$

From Eq.(16) vector  $\mathbf{M}$  is determined, and then according to the angular position of stochastic EM source with respect to the sampling points, the elements of correlation matrix can be calculated using Eq.(18). Matrix elements are normalized with respect to the first matrix element [14]

$$\mathbf{C}_E = \frac{1}{\tilde{C}_{E11}} \cdot \tilde{\mathbf{C}}_E \tag{23}$$

in order to obtain in our considered scenario the correlation matrix that does not depend on value  $r_0$ . For the training of neural network it is sufficient to use only the first row of matrix  $C_E$  ([ $C_{E11}$ ,  $C_{E12}$ , ...,  $C_{E1K}$ ]) due to the fact that this row contains sufficient information for determination of angular coordinates of stochastic sources [14].

### III.B. Neural model for 2D DoA estimation

The neural model, based on MLP ANN, is trained to extract information about position of *S* stochastic sources in azimuth and elevation planes from the correlation matrix  $C_E$  [14]:

$$\begin{bmatrix} \varphi_1 \ \theta_1 \ \varphi_2 \ \theta_2 \dots \ \varphi_s \ \theta_s \ \dots \ \varphi_S \ \theta_S \end{bmatrix}^T = f(\mathbf{C}_E)$$
(24)

where  $[\varphi_1 \ \theta_1 \ \varphi_2 \ \theta_2 \dots \ \varphi_s \ \theta_s \dots \ \varphi_s \ \theta_s]^T$  is vector of spatial angles of arrival of the stochastic sources radiation. The architecture of developed neural model is shown in Fig.9, while Eqs.(8-9) from II.C section are also used here.

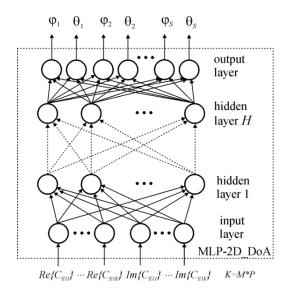


Figure 9: Architecture of MLP neural model for 2D DOA estimation of stochastic EM source signals in *x*-*y* plane [14]

Again as in II.B section, in order to perform mapping it is sufficient to take only the first column of correlation matrix and therefore  $\mathbf{y}_0 = [\text{Re}\{\mathbf{C}_E[1,1]\},..., \text{Re}\{\mathbf{C}_E[1,K]\}, \text{Im}\{\mathbf{C}_E[1,1]\},..., \text{Im}\{\mathbf{C}_E[1,K]\}]$ . Also, output of the neural network model is given as  $[\phi_1 \ \theta_1 \ \phi_2 \ \theta_2 \ \dots \ \phi_8 \ \theta_s \dots \ \phi_8 \ \theta_s]^T = \mathbf{w}_{H+1}\mathbf{y}_H$  where  $\mathbf{w}_{H+1}$  is a connection weight matrix between neurons of last hidden layer and neurons in output layer. The optimization of weight matrices  $\mathbf{w}_1, \mathbf{w}_2,..., \mathbf{w}_H, \mathbf{w}_{H+1}$  and biases values during the training allows ANN to approximate the mapping with the desired accuracy.

## *III.C. 2D DoA estimation - modelling results for uncorrelated sources*

The application of neural model for the 2D DoA estimation of uncorrelated stochastic sources will be illustrated here on the example of one moveable sources (S=1). Stochastic source is represented with an array of two elements (N=2) with isotropic characteristics and with uncorrelated currents supply so that  $\mathbf{c}^{I}$  is the unit diagonal matrix. Signal is sampled in the far-field in nine points that correspond to the rectangular  $M \times P = 3 \times 3$  antenna array  $(K=M\cdot P = 9)$  [13]. Table VI provides the values of parameters for the the scenarios used to generate samples for training the neural models [13]. Sets of samples for training and testing of the MLP models were generated by using Eqs.(18) and (22). Any combination of angles  $\theta$  and  $\varphi$  which is defined by the distribution patterns associated with the vector of 18 elements, represents the first type of signal correlation matrix (9 elements for the real part, and 9 elements in the imaginary part of the complex value of the first type correlation matrix).

 TABLE VI

 The values of parameters used in sampling process [13]

Frequency	f = 22 GHz
Number of antenna array elements per one source	<i>N</i> = 2
Sampling points distance from source trajectory	<i>r</i> <sub>0</sub> = 600 km
Number of sampling points along x axis	<i>M</i> = 3
Mutual distance of the sampling points along x axis	$s = \lambda/2$
Number of sampling points along y axis	<i>P</i> = 3
Mutual distance of the sampling points along <i>y</i> axis	$h = \lambda/2$

 
 TABLE VII

 Testing results for six MLP neural models with the best average errors statistics [13]

MLP model	WCE [%]	ACE [%]
MLP2-15-11	2.52	0.38
MLP2-12-12	2.74	0.39
MLP2-18-14	2.78	0.38
MLP4-13-13	2.79	0.37
MLP2-20-10	2.80	0.38
MLP2-18-7	2.79	0.38



A set of 14641 samples was created for training applying uniform distribution of  $\theta$  and  $\varphi$  with 0.5° step in the range [-30° 30°] and with a 0.5° step. Quazi-Newton method with prescribed accuracy of 10<sup>-4</sup> is used for the training algorithm. Testing set with 7396 samples is providing with uniform distribution of  $\theta$  and  $\varphi$  angles in the range [-30° 30°] with a 0.7° step. The testing results for six MLP models with the lowest average (ACE) and worst case error (WCE) are shown in Table VII, and MLP2-15-11 is chosen as representative neural model. A close agreement between the output values of neural model and referent  $\theta$  and  $\varphi$  values can be observed thorough the scattering diagram of testing samples set shown in Figs.10 and 11 [13].

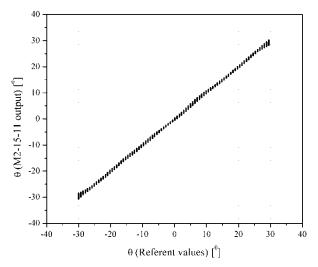


Figure 10: Scattering diagram of MLP2-15-11 model  $\theta$  output [13]

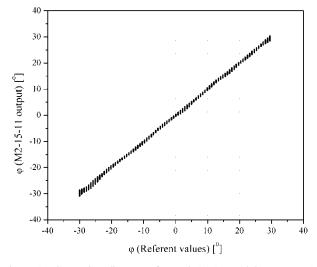


Figure 11: Scattering diagram of MLP2-15-11 model  $\varphi$  output [13]

MLP2-15-11 model was employed to track the movement of the hypothetic stochastic source on earth's surface in a square area in size 800×800 km. The source position was varied along the test trajectory described by the function  $y = 3 \cdot 10^{-6} \cdot (x-10^5)^2 - 3 \cdot 10^5$  where x and y are relative latitude and longitude expressed in meters. Evaluation paths of origin was carried out by sampling in time the correlation matrix of the 69 points shown in Figure 12 [13]. A satisfactory agreement can be observed between the values of the source positions which war estimated by the neuron model and the referent source trajectory.

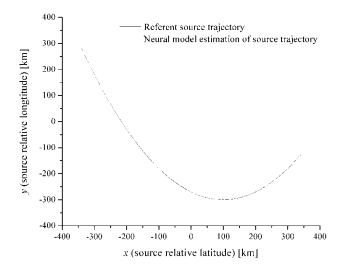


Figure 12: A simulation of localization and tracking the movement of the hypothetic source of stochastic radiation on earth's surface with the MLP2-15-11 model [13]

### IV. CONCLUSION

Overview of using MLP ANNs for the localization of stochastic EM sources was given in the paper. It was illustrated that the develop neural models can be used for efficient and accurate 1D and 2D estimation of electromagnetic radiation originating from either uncorrelated or partially correlated stochastic sources. Future research will be focused to the more general 2D DOA estimation of multiple stochastic sources with different signal level and at arbitrary angular and radial distances from the reception point.

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