The Optimization of the STOI Algorithm Parameters in Presence of the White Gaussian Noise (WGN)

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Abstract – The first part of the paper describes the Short Time Objective Intelligibility - STOI algorithm, which makes an objective evaluation of intelligibility, as well as an algorithm for estimating the optimal parameters of the STOI algorithm, N and β. Second part of the paper, described an experiment that examines the intelligibility of the sentences formed from the Serbian Matrix Sentence Test - SMST base using: a), subjective MOS (Mean Opinion Score) test and b), objective test STOI algorithm. Subsequently, a comparative analysis of the results were made and it was determinate an analytical formula which connecting optimal pairs (N, β). Using the results of the MOS test as a reference, a mean absolute error of estimation of the STOI algorithm was determined.

Keywords – Intelligibility, Objective Measure, STOI, MOS.

I. INTRODUCTION

When designing audio systems for speech transfer, one of the most important features should be predicted - intelligibility of speech, taking care about one-third octave band. In speech technology, term "intelligibility", is ranging from 0 to 100% intelligibility. Intelligibility of phoneme identification by listeners is a direct measure of intelligibility. The intelligibility of speech is the property of a speech signal that can be measured using: subjective and objective methods.

Subjective methods of evaluation intelligibility are realized with the MOS test. These tests are often long-lasting and cost very well. They are realized using different sets of word (logatoms [1], Phonetic Balansed [2]...) and sentences (everyday [3] and matrix [4]).

Objective methods for evaluation intelligibility implies speech tests are carried out using a computer. Parameters such as: AI [5], SII [6], STI [7], CSTI [8] are used for testing. They are suitable for evaluation of intelligibility of speech for several types of degradation: reverberation, additive noise, filtering and clipping.

AI is an articulation index developed in the AT & Bell Labs [5]. Based on AI the speech intelligibility index - SII was developed [6]. Following the index SII, Hou gast and Steeneken developed a speech transfer index - STI [7], which can predict the intelligibility of reverberated speech and nonlinearity of distortion.

However, if we want to make an objective evaluation of intelligibility using a method where the disorder signal is processed by some kind of time-frequency variable (TF) gain function, these are not appropriate methods.

In the paper [9], STOI algorithm for objective testing of sentences was demonstrated. The work is based on the analysis of the speech signal in the time frequency domain (TF). The efficiency of the STOI algorithm was tested under the conditions of a superposed noise: car, caffe and bottle.

In this paper, the effectiveness of the STOI algorithm was analyzed in evaluation the intelligibility of sentences spoken in the Serbian language in the presence of the variable level of the White Gaussian Noise (WGN). The authors created an algorithm for determining the optimal parameters of the STOI algorithm (Nopt, βopt). The experiment was realized at the Collage of Applied Technical Science in Niš in which it was performed: a). subjective MOS test and b). an objective test using the STOI algorithm. The experiment was realized for SNR = [-7, -5, -2, 0, 2] dB. The tests were implemented on students of the Collage of Applied Technical Science in Niš, gender structure: 10 male and 10 female, age from 19 to 26 years. The subjective MOS test determined the intelligibility of sentences spoken in the Serbian language and was used as a reference for the purpose of comparing the results obtained with the STOI algorithm. Comparative analysis of the results determined the optimal parameters of the STOI algorithm Nopt, βopt, as well as their analytical dependence. In the end, a mean absolute error of estimation of the STOI algorithm was determined, for measuring the results obtained by the MOS test.

The organization of work is the follow. Section II describes the STOI algorithm. Section III describes the algorithm for evaluation of optimal parameters. Section IV describes an experiment of evaluation intelligibility and performs comparative analysis of the results. Section V is a conclusion.

II. STOI ALGORITHM

The STOI algorithm is described in [9] and consists of the following steps:

Input: x - clean speech signal, y - speech signal with superimposed noise, Output: d - intelligibility.

Step 1: TF decomposition of the x and y signals.

Step 2: Forming frames of length 256 and modification using the Hann - windowed.

Step 3: Removing the silence regions.

Step 4: Find the frame with the maximum energy of signal x.

Step 5: Finding the kth DFT-bin of the mth frame. The standard of one-third octave is defined as:
where \( k_1 \) and \( k_2 \) represented the boundaries of one-third octave.

**Step 6:** Forming a short-time envelope vector of clean signal:
\[
x_{j,m} = [x_j(m - N + 1), X_j(m - N + 2), ..., X_j(m)]^T,
\]
where \( N = 30 \), which corresponds to a frame length of 384 ms, for \( f_s = 10 \text{ kHz} \).

**Step 7:** The normalization and clipping of \( y \) signal
\[
y_{j,m}(n) = \min \left( \left\{ \frac{x_{j,m}}{y_{j,m}} \right\}, 1 + 10^{-\beta/20}x_{j,m}(n) \right),
\]
where \( \beta = -15 \text{ dB} \).

**Step 8:** Defining a measure of intelligibility \( d_{j,m} \):
\[
d_{j,m} = \left( x_{j,m} - \mu_{y,m} \right) \left( y_{j,m} - \mu_{y,m} \right)
\]
\[
\left\{ \frac{x_{j,m} - \mu_{y,m}}{y_{j,m} - \mu_{y,m}} \right\}.
\]

**Step 9:** The average measure of intelligibility for all bands and frames is \( d \):
\[
d = \frac{1}{JM} \sum_{j,m} d_{j,m},
\]
where \( M \) represent total number of frames, and \( J \) number of one-third octaves.

## III. ALGORITHM FOR EVALUATION OF OPTIMAL PARAMETERS

The algorithm for determining the optimal parameters of the STOI algorithm is realized in the following steps:

**Input:** \( SNR_{\text{min}}, SNR_{\text{max}}, SNR_{\text{SNR}}, \beta_{\text{min}}, \beta_{\text{max}}, \Delta \beta, N_{\text{min}}, N_{\text{max}}, \Delta N, N_r \).

**Output:** trajectory of optimal values \( y_{\text{fit}} \).

**Step 1:** Created the test of sentence, with fixed syntax word structure from the SMST base (signal \( x_k \)).

**FOR** \( SNR = SNR_{\text{min}} \): \( \Delta SNR \): \( SNR_{\text{max}} \)

**FOR** \( r = 1 : N_r \),

**Step 2:** Superposed White Gaussian noise, \( n \) (\( \sigma^2 = 1, \mu = 0 \))
\[
x_{i,r} = x_i + k_i \cdot n,
\]
where \( k_i \) is the coefficient determining the SNR of the speech signal \( x_i \).

**Step 3:** Realization of a subjective MOS test and generating an evaluation of intelligibility MOSxr.

**FOR** \( \beta = \beta_{\text{min}} : \Delta \beta : \beta_{\text{max}} \)

**FOR** \( N = N_{\text{min}} : \Delta N : N_{\text{max}} \)

**Step 4:** Application of STOI algorithm
\[
d, (N, \beta) = \text{STOI} (N, \beta)
\]

**END \( N \);**

**END \( \beta \);**

**Step 5:** Forming of equivalent matrix of intelligibility coefficient:
\[
d(N, \beta) = \delta_r(N, \beta),
\]

**Step 6:** The mean value of coefficient for STOI intelligibility is:
\[
d_{\text{STOI}} = \delta(N, \beta),
\]
and statistical parameters are mean value \( \mu = d_{\text{STOI}} \) and variance \( \sigma^2 \).

**Step 7:** Forming matrix error of evaluation:
\[
e = |d - MOS_{\mu}|,
\]

**Step 8:** Generating a trajectory of minimum error:
\[
y_{\text{fit}} = f(N_{\text{opt}}, \beta_{\text{opt}}).
\]

**Step 9:** Generating an equivalent trajectory of optimal values by fitting method:
\[
y_{\text{fit}} = \beta_{\text{fit}} = a_3N^3 + a_2N^2 + a_1N + a_0,
\]
where \( a_3 = -4.927 \times 10^{-5}, a_2 = 0.01177, a_1 = -0.9856, a_0 = 2.942 \).

## IV. EXPERIMENTAL RESULTS AND ANALYSIS

In this section, an experiment was implemented in order to find the optimal parameters of the STOI algorithm.

### A. Experiment

In order to test the effectiveness of evaluation using the STOI algorithm, experiment was implemented at the Collage of Applied Science Niš, where is applied a algorithm described in Section III for the evaluation of intelligibility. An experiment was implemented in order to find the optimal parameters of the STOI algorithm. The input parameters are:

a). \( SNR_{\text{min}} = -7 \text{ dB}, SNR_{\text{max}} = 2 \text{ dB}, \Delta SNR = 2 \text{ dB} \), b). \( N_r = 20 \), number of test sentences for each value \( SNR \), c). \( N_{\text{min}} = 10, N_{\text{max}} = 100, \Delta N = 10, \beta_{\text{min}} = -40, \beta_{\text{max}} = -5, \Delta \beta = 5 \). The output parameters of the algorithm are:

a) analytic function of optimal values \( \beta_{\text{opt}} = y_{\text{fit}} \), b) the results of subjective test \( MOS_{\mu} \), c). the results of objective test \( d_{\text{STOI}} \) i d), statistical parameter: mean value \( \mu \) and variance \( \sigma^2 \) for \( d_{\text{STOI}} \). Results are shown in tabular and graphical form.

### B. The base

A SMST base has been created which contains words (name, verb, number, adjective and object) spoken in Serbian language [10]. Using the algorithm described in section III

360
(step 1), sentences with a fixed syntax structure were formed. The words are formed by a random selection of the word from the SMST base to the syntax structure: name-verb-number-adjective-object. It is possible to create 100000 different sentences, which made test unpredictable for the tested group.

C. Test group

A test group was formed from students of the Collage of Applied Science Nis, age from 19 to 26 (μ = 20.85), gender structure: 10 male and 10 female respondents.

D. The results

Table 1 shows the results of MOS (step 3) and dSTOI (step 4) and statistical of mean values μ and variance σ² for various SNR values.

The values of the MOS and STOI coefficients for each sentence are shown graphically for: a) SNR = 0 dB (Figs. 1.a) and b) SNR = -7 dB (Figs. 2.a). The value of equivalent matrix coefficients d(N, β), (step 5) are shown: a) SNR = 0 dB (Figs. 1.b) and b) SNR = -7 dB (Figs. 2.b). A matrix error of intelligibility evaluation e (step 7) are shown: a) SNR = 0 dB (Figs. 1.c) and b) SNR = -7 dB (Figs. 2.c). Trajectories of minimal error of intelligibility evaluation yβ (N, β), (step 8) are shown on: a) SNR = 0 dB (Figs. 1.d) and b) SNR = -7 dB (Figs. 2.d). In Fig. 3 are shown: a) trajectory yβ minimal error for SNR = {-7, -5, -2, 0, 2} dB and b) equivalent trajectory yβe (step 9). Intelligibility determined with: a) subjective MOS test, MOSv, and objective test using STOI algorithm, dSTOI, are shown in Fig. 4.

<table>
<thead>
<tr>
<th>SNR (dB)</th>
<th>MOSv (%)</th>
<th>σ²</th>
<th>μ (%)</th>
<th>dSTOI</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>71</td>
<td>4.4834</td>
<td>70.1975</td>
<td>70.1975</td>
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<tr>
<td>0</td>
<td>61</td>
<td>4.8871</td>
<td>66.5205</td>
<td>66.5205</td>
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<tr>
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<td>57</td>
<td>5.0465</td>
<td>61.5471</td>
<td>61.5471</td>
</tr>
<tr>
<td>-5</td>
<td>47</td>
<td>538.5059</td>
<td>45.0886</td>
<td>45.0886</td>
</tr>
<tr>
<td>-7</td>
<td>34</td>
<td>364.4125</td>
<td>44.0291</td>
<td>44.0291</td>
</tr>
</tbody>
</table>

![Graph 1](image1.png)

![Graph 2](image2.png)

![Graph 3](image3.png)
By analysis of results shown in Table I and Figs. 1 ÷ 4, it can be concluded that:

\[ e_{SNR} = \frac{1}{5} \sum_{SNR=7dB}^{2dB} |MOS_{XR}(SNR) - d_{STOI}(SNR)| = 4.5622\% \]

which is considered a good evaluation.

V. CONCLUSION

The paper presents an algorithm for determining the optimal parameters of the STOI algorithm in the presence of WGN. A detailed analysis of the results of the conducted experiment showed that there are an infinitely large number of values of optimal parameters and their analytical formula is determined. Taking into account the results of the subjective MOS test as a reference, it has been shown that the mean absolute error of evaluation intelligibility of the STOI algorithm is \( e_{SNR} = 4.5622\% \). This result points to the quality of the STOI algorithm and makes recommendations for its application when evaluating speech intelligibility.

REFERENCES